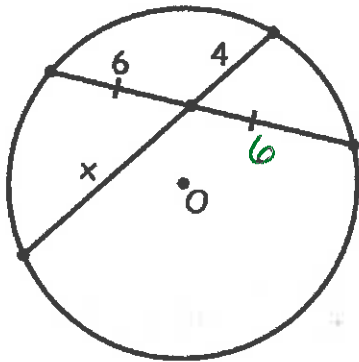


Chords, Tangents & Secants – Segment Lengths

Theorem: If 2 chords intersect **inside** a circle, then the **products of their parts** are =.

Example:



$$4(x) = 6(6)$$

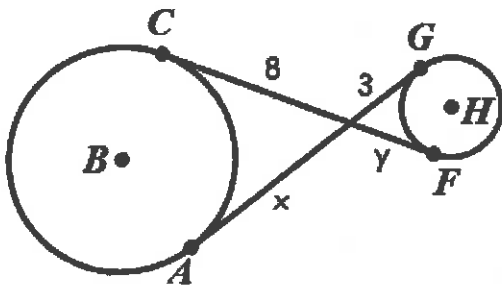
$$4x = 36$$

$$x = 9$$

Theorem: If 2 tangents intersect **outside** a circle, then they are **congruent**.

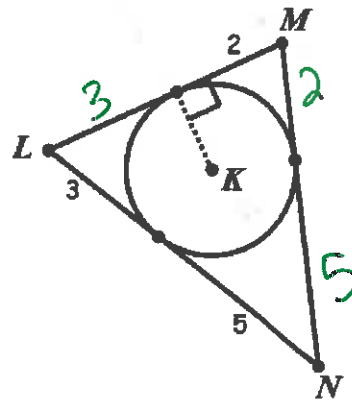
This is often called the Ice Cream Cone Theorem.

Examples:



$$x = 8$$

$$y = 3$$



$$\text{Perimeter} = 10 + 4 + 6$$

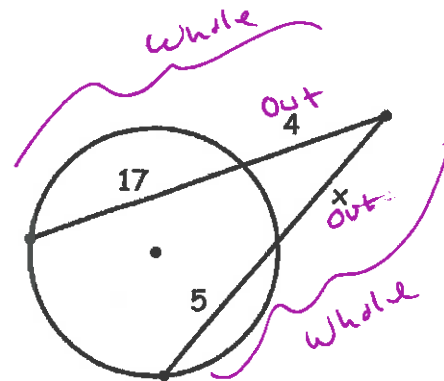
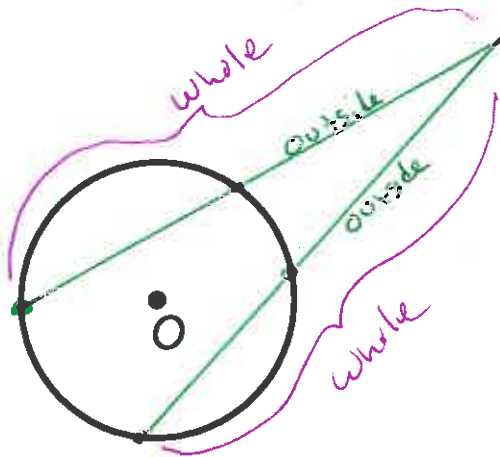
$$= 20$$

Theorem: If two secants or one secant and one tangent intersect **outside** a circle then:

$$(\overset{\text{Full}}{\text{Whole Segment}})(\overset{\text{out}}{\text{Outside part}}) = (\overset{\text{Full}}{\text{Whole Segment}})(\overset{\text{out}}{\text{Outside part}})$$

Secant-Secant:

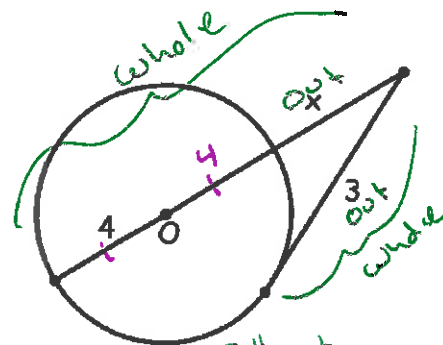
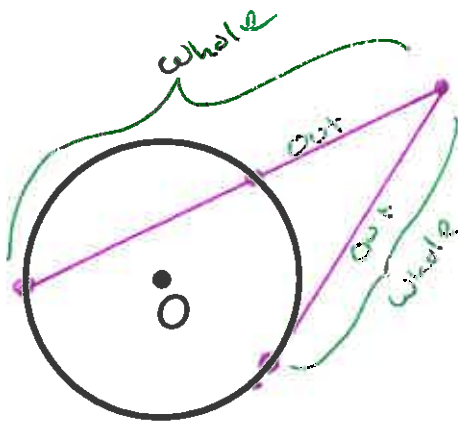
Examples:



$$\begin{aligned}
 21(4) &= (5+x)x \\
 84 &= 5x + x^2 \\
 x^2 + 5x - 84 &= 0 \\
 (x+12)(x-7) &= 0 \\
 \text{reject } x &= -12, \quad x = 7
 \end{aligned}$$

Secant-Tangent:

Examples:



$$\begin{aligned}
 (8+x)x &= 3(3) \\
 8x + x^2 &= 9 \\
 x^2 + 8x - 9 &= 0
 \end{aligned}$$

$$\begin{aligned}
 (x+9)(x-1) \\
 \text{reject } x &= -9, \quad x = 1
 \end{aligned}$$